

# HELSA: Hierarchical Reinforcement Learning with Spatiotemporal Abstraction for Large-Scale Multi-Agent Path Finding



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TONGJI UNIVERSITY

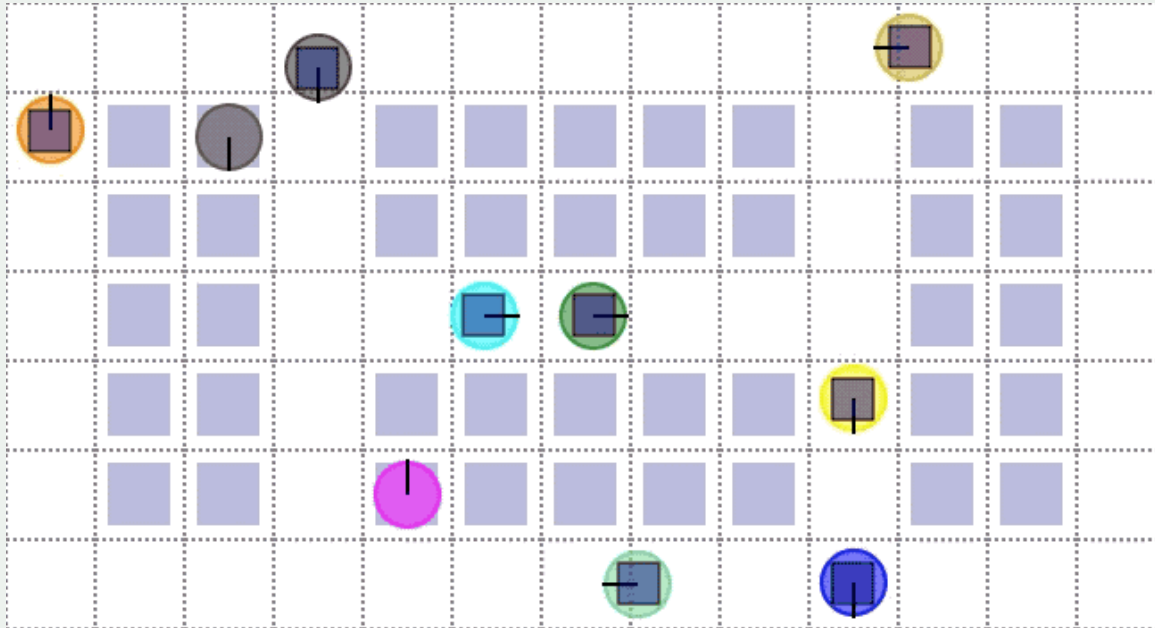


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# Background

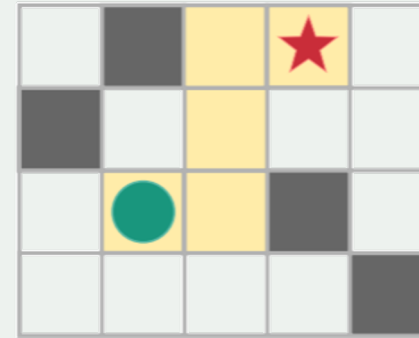
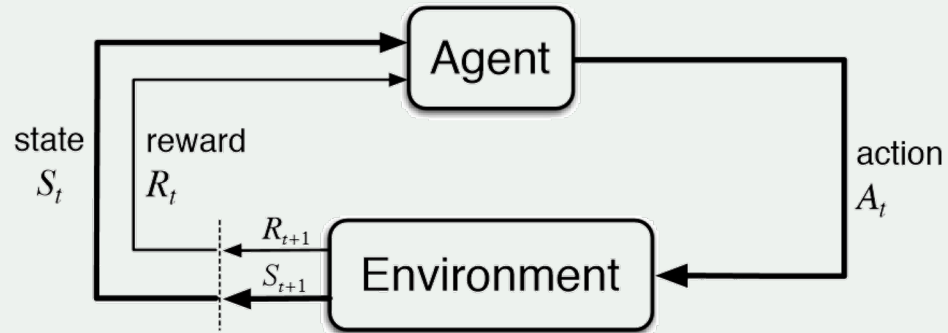
## The Multi-Agent Pathfinding (MAPF) Problems



\* Images retrieved from <https://www.cs.sfu.ca/~hangma/>, Amazon Robotics and SuperStock.

# Key Challenges

## Sparse Rewards in Large-scale Reinforcement Learning



$$R(\mathbf{a}) = \mathbb{1}[\text{Execute}(\cdot, \mathbf{a}) = \star]$$

$$\mathbf{a}_1 = (\rightarrow, \uparrow, \uparrow, \rightarrow)$$

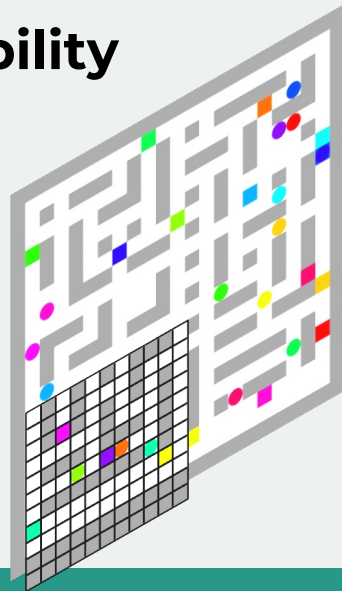
$$\mathbf{a}_2 = (\leftarrow, \rightarrow, \rightarrow, \uparrow, \uparrow, \rightarrow)$$

$$\mathbf{a}_3 = (\uparrow, \rightarrow, \rightarrow, \uparrow)$$

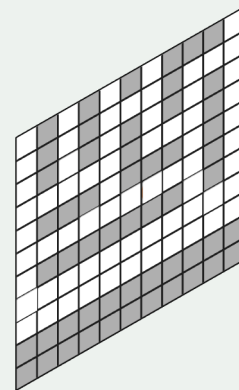
$$R(\mathbf{a}_1) = R(\mathbf{a}_2) = R(\mathbf{a}_3) = 1$$

## Partial Observability

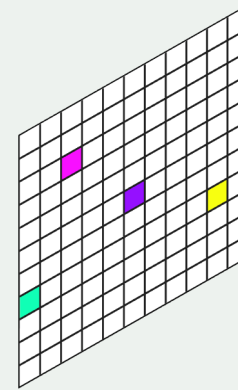
Grid world



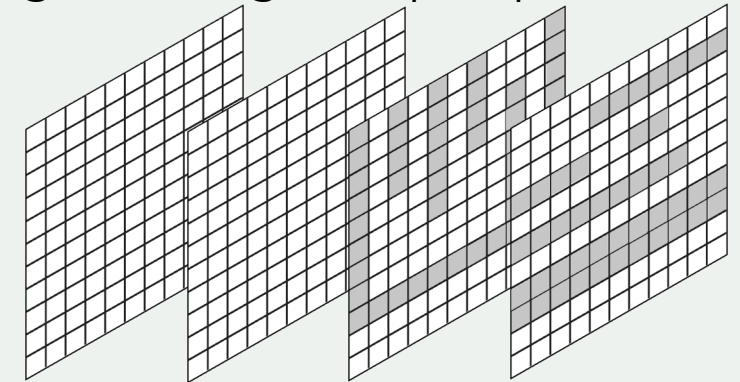
Observation encodings from agent's perspective



Obstacles



Agents



Heuristic Maps



# Overview

## Solution: Hierarchical Reinforcement Learning

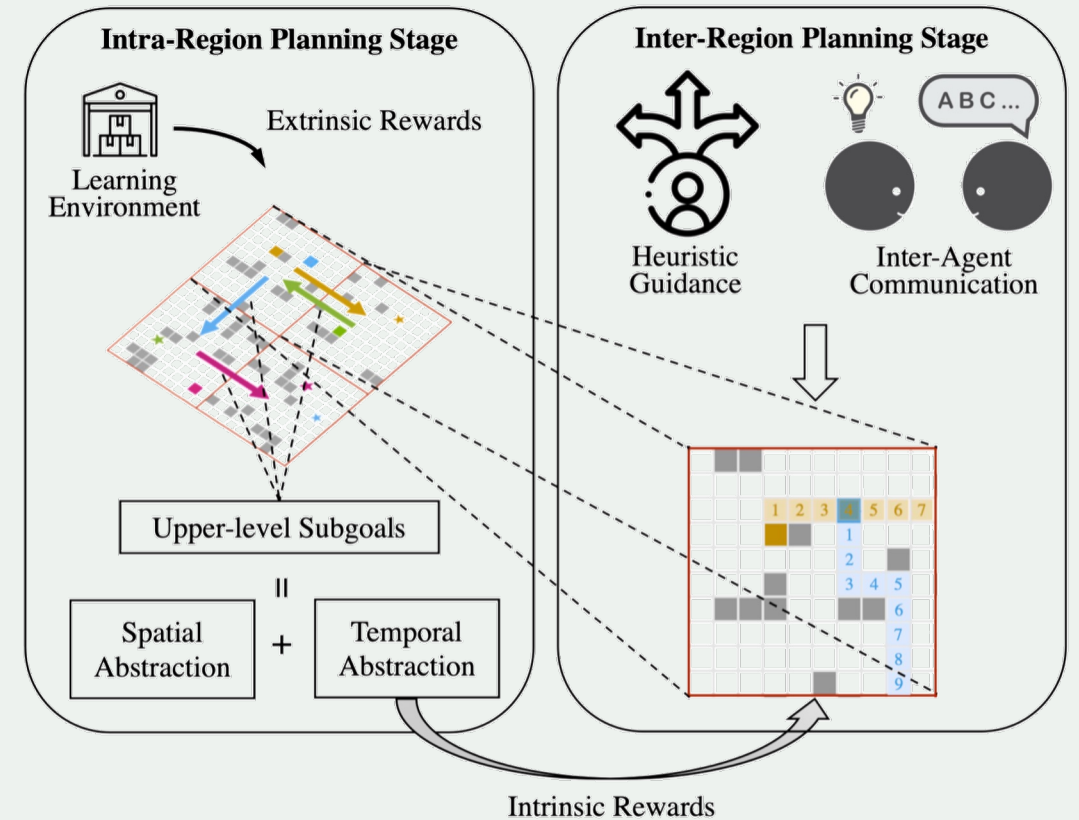
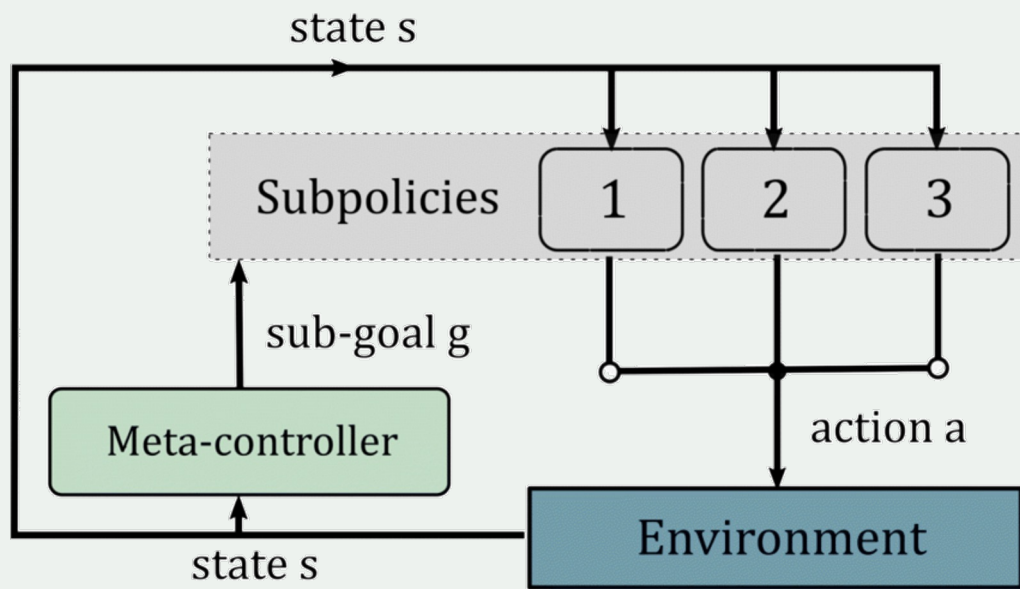


Fig. 1: Illustration of the HELSA framework

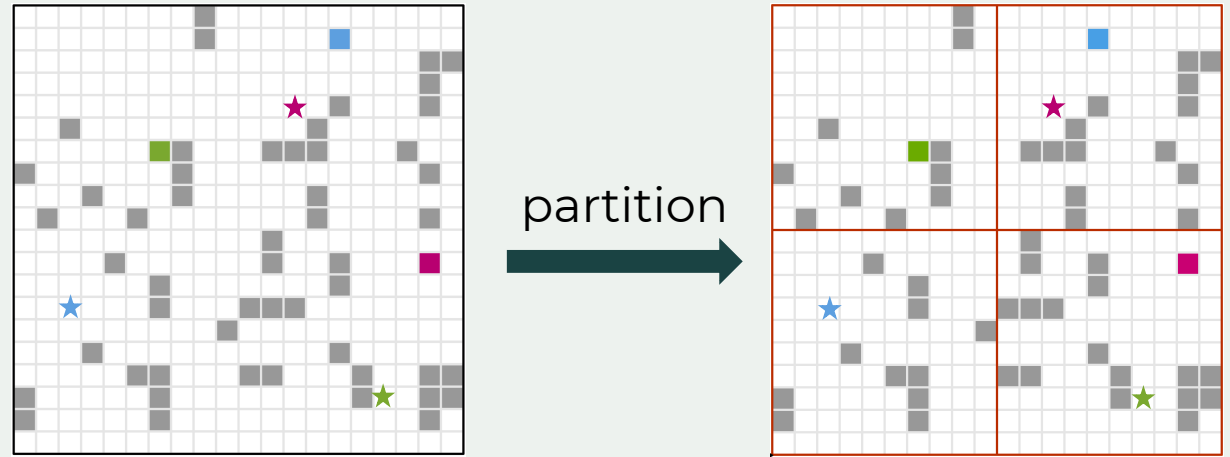




# The Proposed Framework

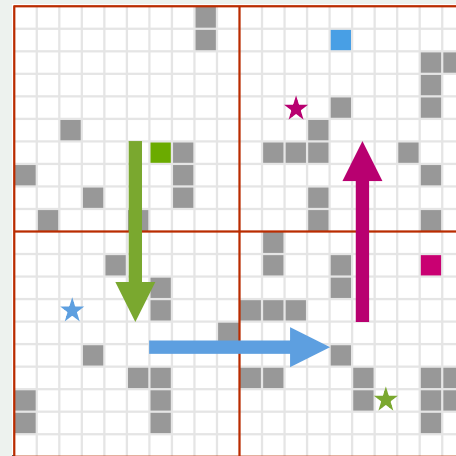
## 01 Map Partition

**Divide** the space into a series of **regions** based on hyperparameters.



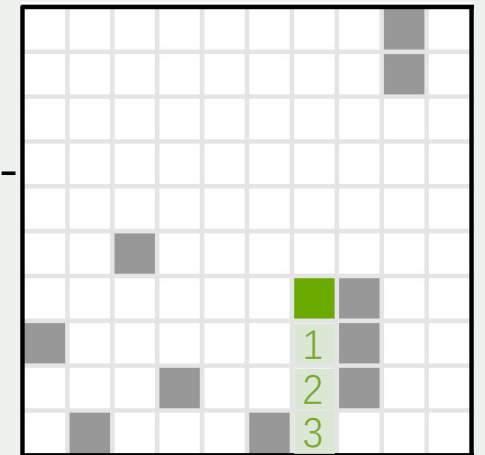
## 02 Temporal Abstraction

**Decompose** long-term tasks on a temporal scale into **short-term tasks**



## 03 Subtask Solver

**Solve** constrained multi-goal multi-agent pathfinding problems



# Lower-Level Controller

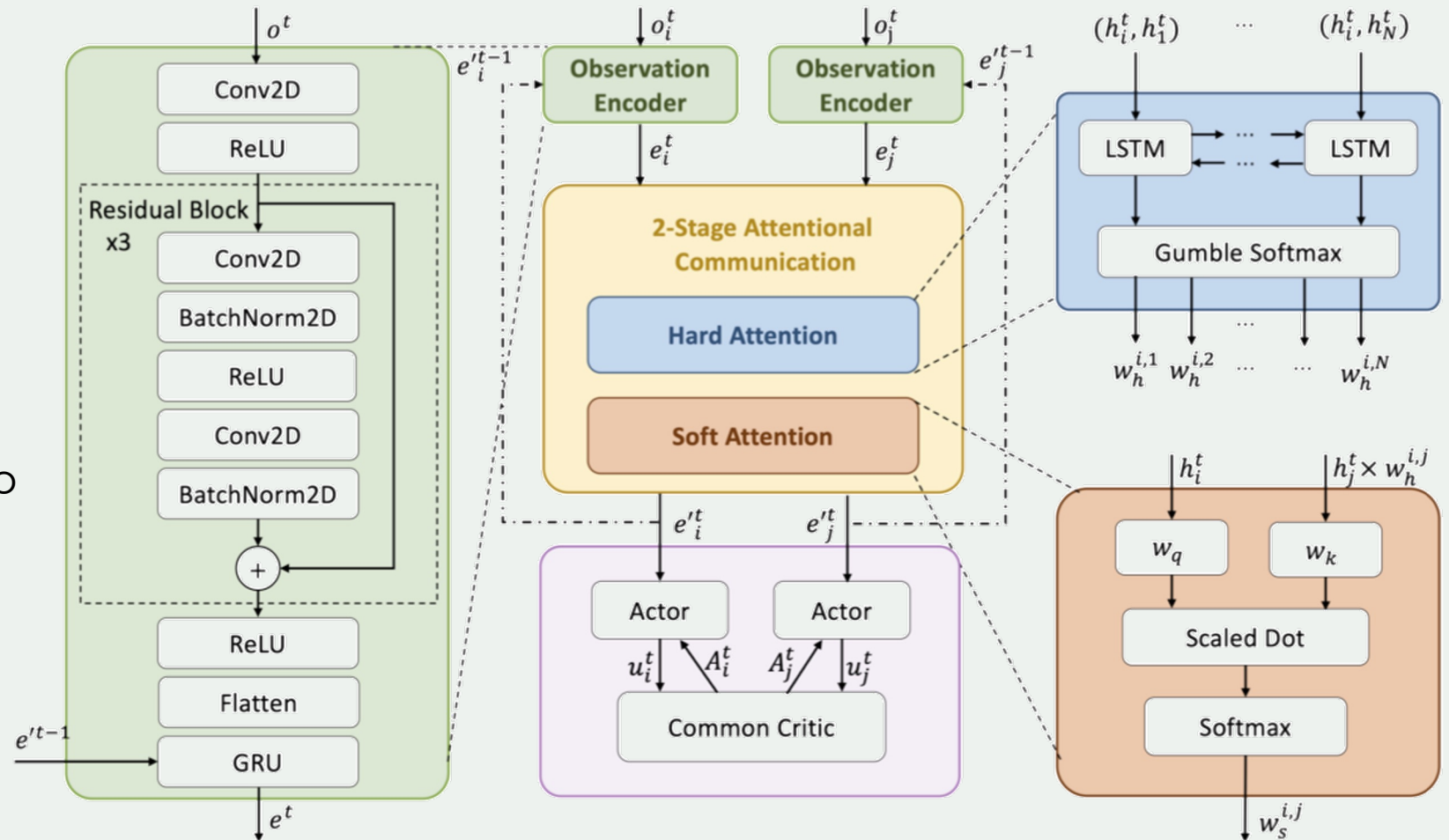
## Observation Encoder

- Agents positions
- Obstacle positions
- Heuristic encodings
- Last-step messages

## Communication Block

- Hard attention mechanism to filter out irrelevant agents
- Soft attention to calculate relative importance

## Action Network

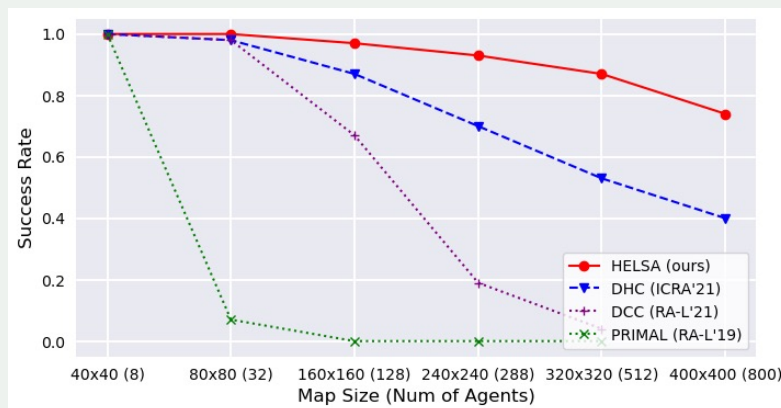


# Empirical Analysis on Randomly Generated Datasets

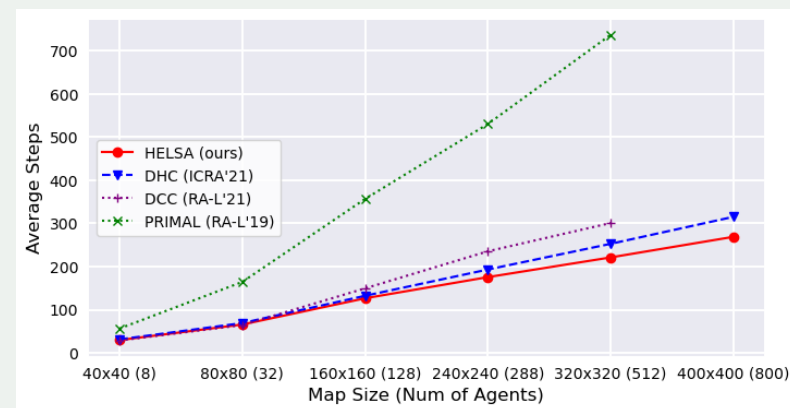
## ➤ Evaluation Metrics

- Success Rates
- Average Steps
- Makespans
- Collisions with Agents
- Collisions with Obstacles

## ➤ Success Rates



## ➤ Average Steps



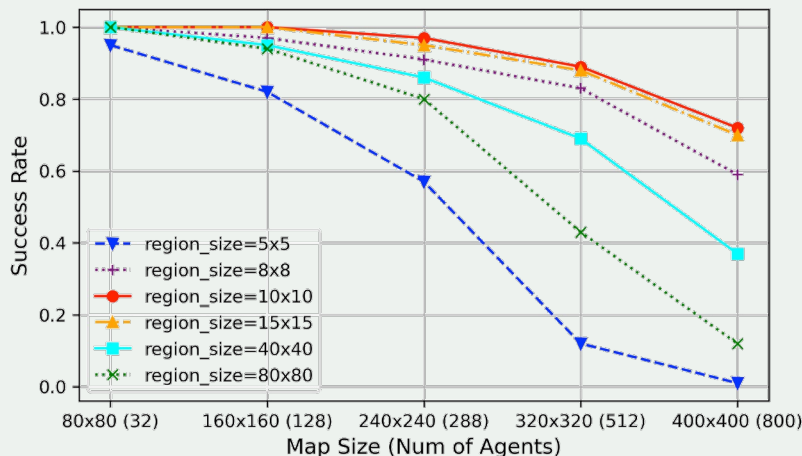
Model	8 agents, 40-sized map, 0.2 density					32 agents, 80-sized map, 0.2 density					128 agents, 160-sized map, 0.2 density				
	SR ↑	AS ↓	MS ↓	CA ↓	CO ↓	SR ↑	AS ↓	MS ↓	CA ↓	CO ↓	SR ↑	AS ↓	MS ↓	CA ↓	CO ↓
PRIMAL [4]	1.0	56.49	98.90	0.42	0.0	0.88	164.39	305.73	4.12	0.0	0.07	356.51	1007.08	113.06	4.27
DHC [6]	1.0	31.40	55.77	0.38	0.0	0.98	69.18	139.77	3.20	0.0	0.87	132.31	399.19	29.38	0.06
DCC [7]	1.0	<b>28.84</b>	<b>50.49</b>	0.40	0.0	0.98	<b>64.47</b>	<b>134.34</b>	5.91	0.01	0.67	149.50	567.41	37.48	0.0
HELSA	<b>1.0</b>	29.71	52.29	<b>0.21</b>	<b>0.0</b>	<b>1.0</b>	65.85	136.17	<b>0.54</b>	<b>0.0</b>	<b>0.97</b>	<b>126.51</b>	<b>296.14</b>	<b>3.69</b>	<b>0.0</b>
Model	288 agents, 240-sized map, 0.2 density					512 agents, 320-sized map, 0.2 density					800 agents, 320-sized map, 0.2 density				
	SR ↑	AS ↓	MS ↓	CA ↓	CO ↓	SR ↑	AS ↓	MS ↓	CA ↓	CO ↓	SR ↑	AS ↓	MS ↓	CA ↓	CO ↓
PRIMAL [4]	0.0	530.06	1536.0	593.59	34.48	0.0	736.50	2048.0	1498.20	173.49	-	-	-	-	-
DHC [6]	0.70	193.13	804.55	99.52	<b>0.01</b>	0.53	252.62	1304.48	236.22	0.30	0.40	315.08	1906.36	468.61	0.71
DCC [7]	0.19	235.32	1375.04	151.88	12.97	0.04	300.78	2020.76	423.40	57.41	-	-	-	-	-
HELSA	<b>0.93</b>	<b>175.56</b>	<b>629.58</b>	<b>49.41</b>	0.03	<b>0.87</b>	<b>221.17</b>	<b>935.99</b>	<b>101.78</b>	<b>0.04</b>	<b>0.74</b>	<b>268.83</b>	<b>211.15</b>	<b>269.67</b>	<b>0.37</b>

# Empirical Analysis

How does the partitioning granularity effect the performance of HELSA?

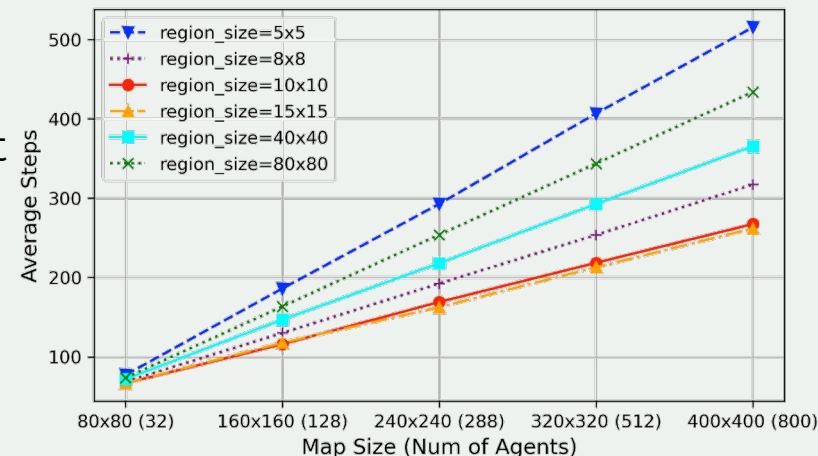
➤ **Success Rates**

Perform best at approximately 10x10 – 15x15 region size



➤ **Average Steps**

Perform best at approximately 10x10 – 15x15 region size



Does the two-stage attention communication lead to better coordination?

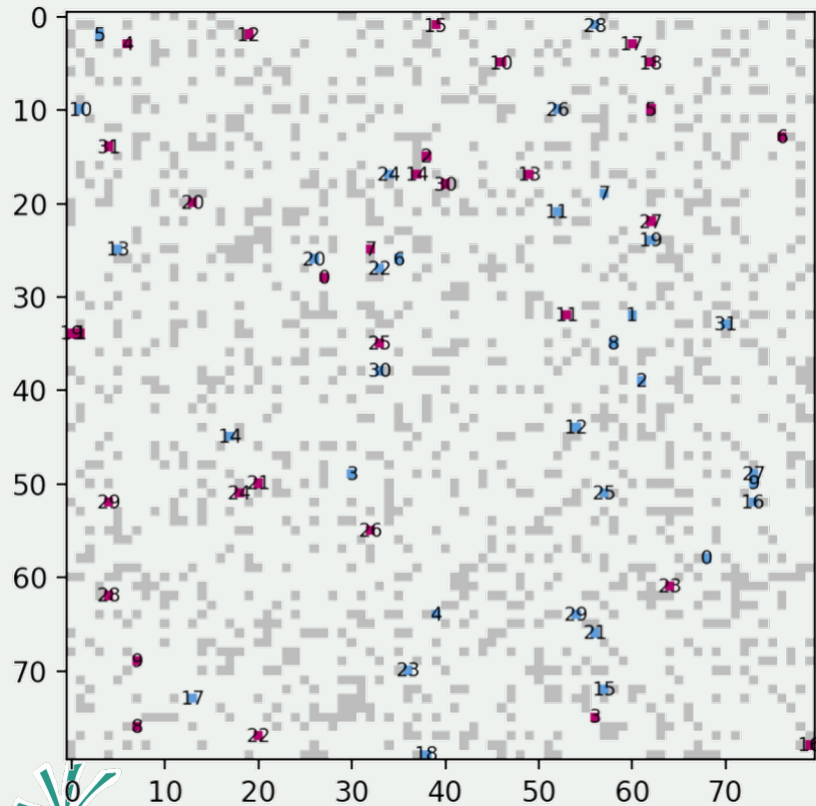
TABLE III: Evaluation of the adopted lower-level controller with other ablations in terms of success rates and average steps.

Method	w/ hierarchy?	80-sized map		160-sized map		240-sized map		320-sized map		400-sized map		Avg.	
		SR ↑	AS ↓	SR ↑	AS ↓	SR ↑	AS ↓	SR ↑	AS ↓	SR ↑	AS ↓	SR ↑	AS ↓
COMA+Comm +Attention	✓	<b>1.0</b>	<b>65.85</b>	<b>0.97</b>	<b>126.51</b>	<b>0.93</b>	<b>175.56</b>	<b>0.87</b>	221.17	0.74	268.83	<b>0.90</b>	<b>171.58</b>
		0.98	67.25	0.76	141.95	0.41	219.03	0.07	287.99	0.0	347.63	0.44	212.77
COMA+Comm	✓	<b>1.0</b>	66.78	0.95	130.20	0.90	182.13	0.86	<b>219.75</b>	<b>0.77</b>	<b>245.00</b>	0.90	172.97
		0.98	69.89	0.72	147.77	0.35	233.98	0.09	311.93	0.0	387.54	0.43	230.22
COMA	✓	0.95	96.30	0.83	193.39	0.44	323.95	0.04	433.73	0.0	615.19	0.45	332.51
		0.90	139.13	0.43	248.67	0.12	477.53	0.01	633.55	0.0	883.10	0.29	476.40

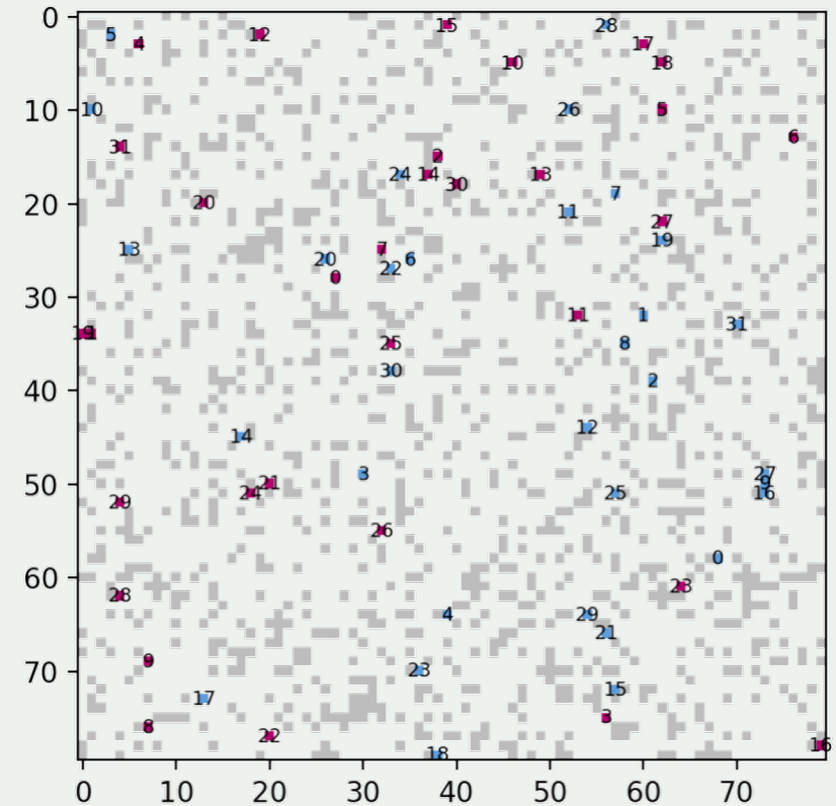


# Simulation Results

HELSA w/ hierarchical controllers



HELSA w/ only low-level controllers

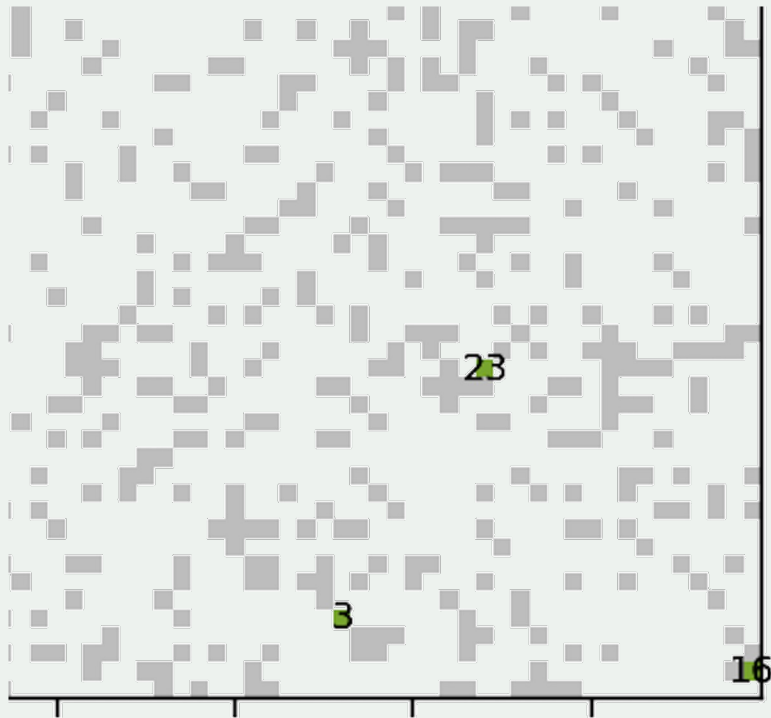


80x80-sized map, 32 agents, 20% obstacle density



# Simulation Results

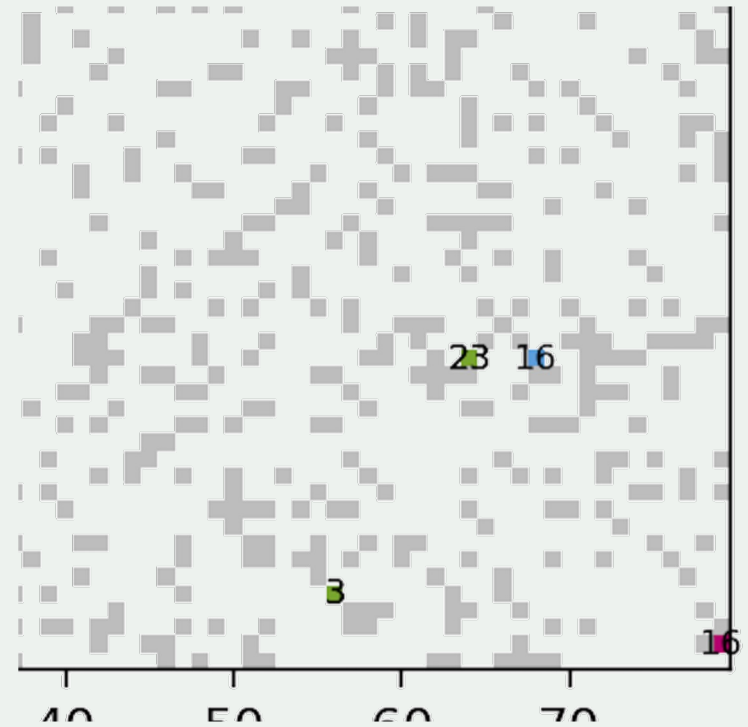
HELSA w/ hierarchical controllers



GOOD Case!

Succeeded at 122<sup>th</sup> step

HELSA w/ only low-level controllers



BAD Case!

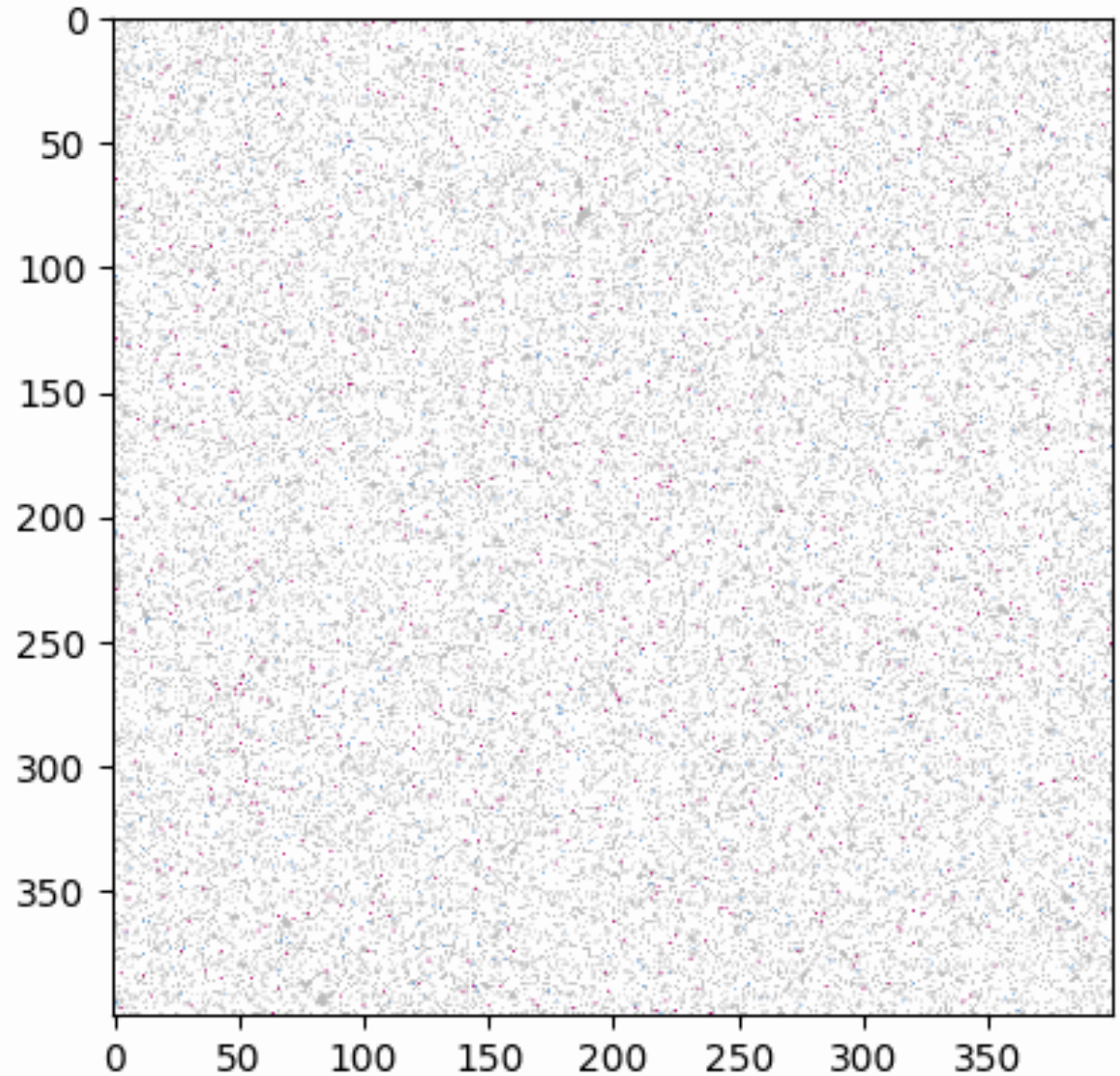
Agent 16 failed its job



# Simulation Results

Showcase of a challenging  
400x400-sized scenario, with 800  
agents and 32,000 obstacles

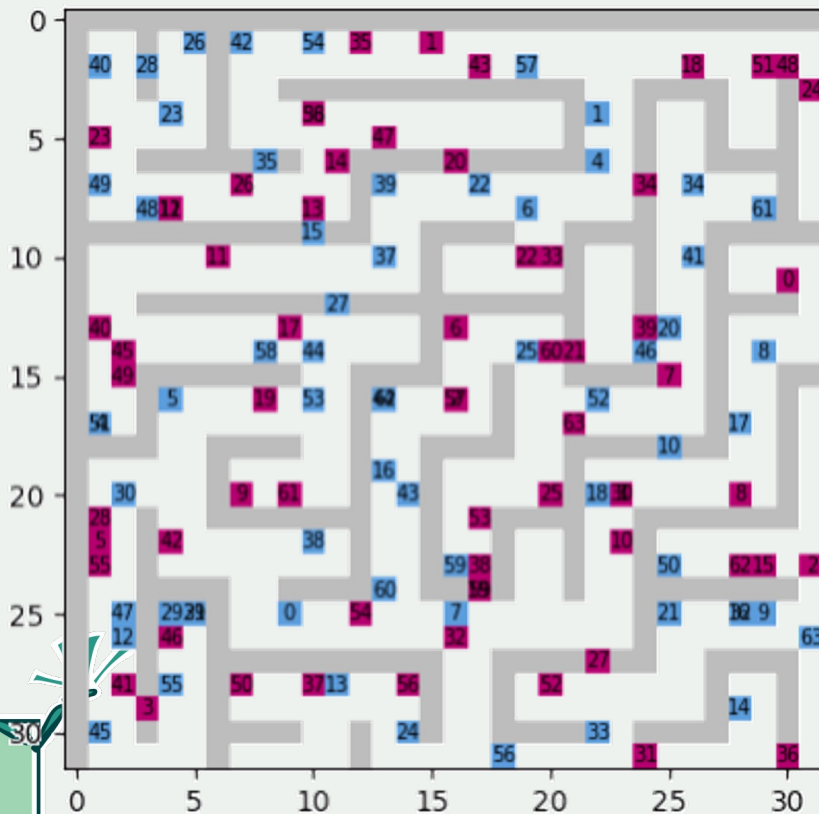
All agents reach their destinations  
at the 746<sup>th</sup> timestep



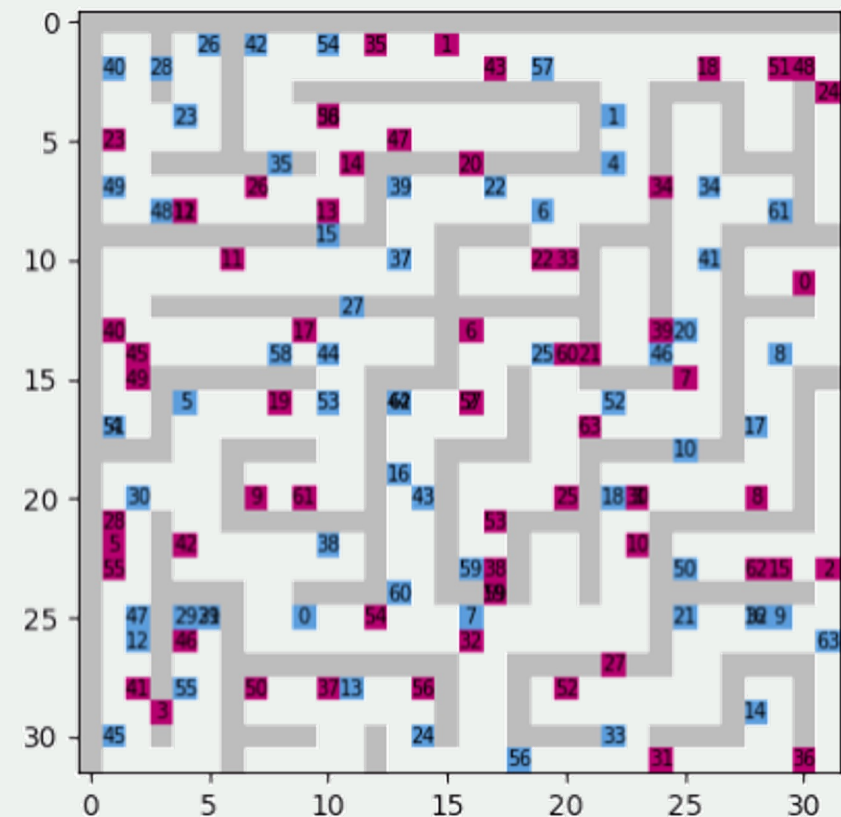
# Simulation Results

maze-32-32-2 from mapf.info (SoCS'19, a challenging benchmark), 64 agents

HELSA



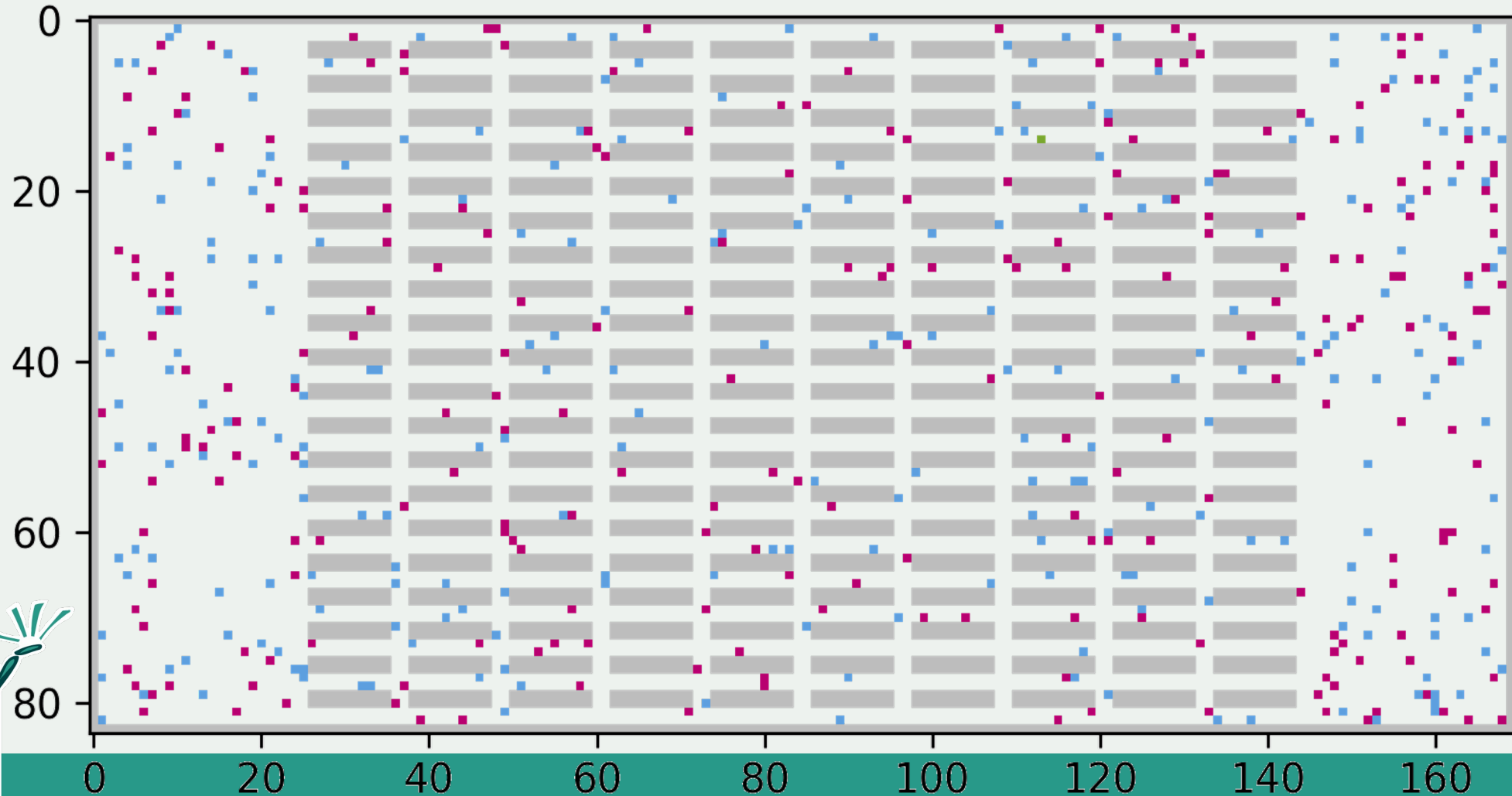
DCC (R-AL' 21)





# Simulation Results

warehouse-10-20-10-2-2 from mapf.info (SoCS'19), 256 agents



# Thanks for Listening!



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